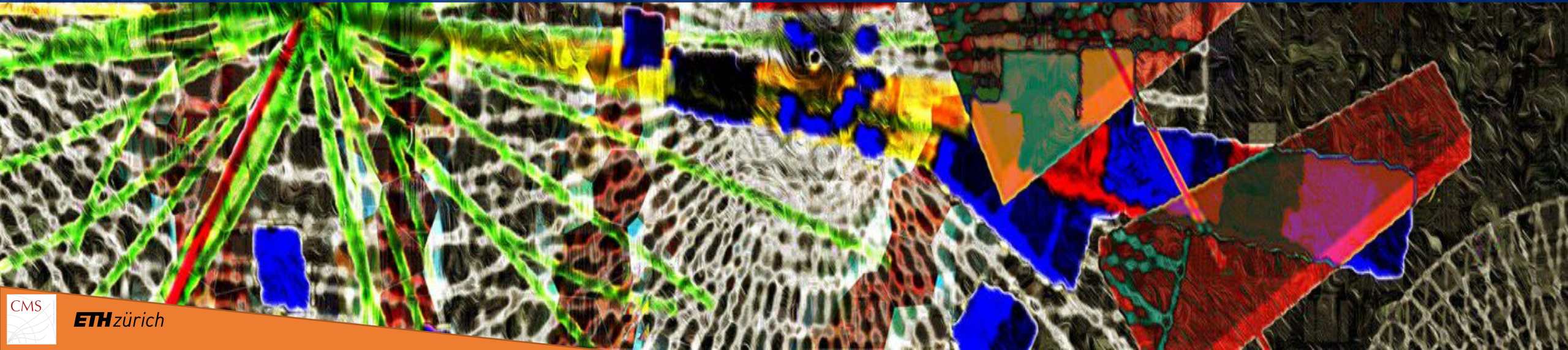


Electromagnetic Shower Corrections in CMS

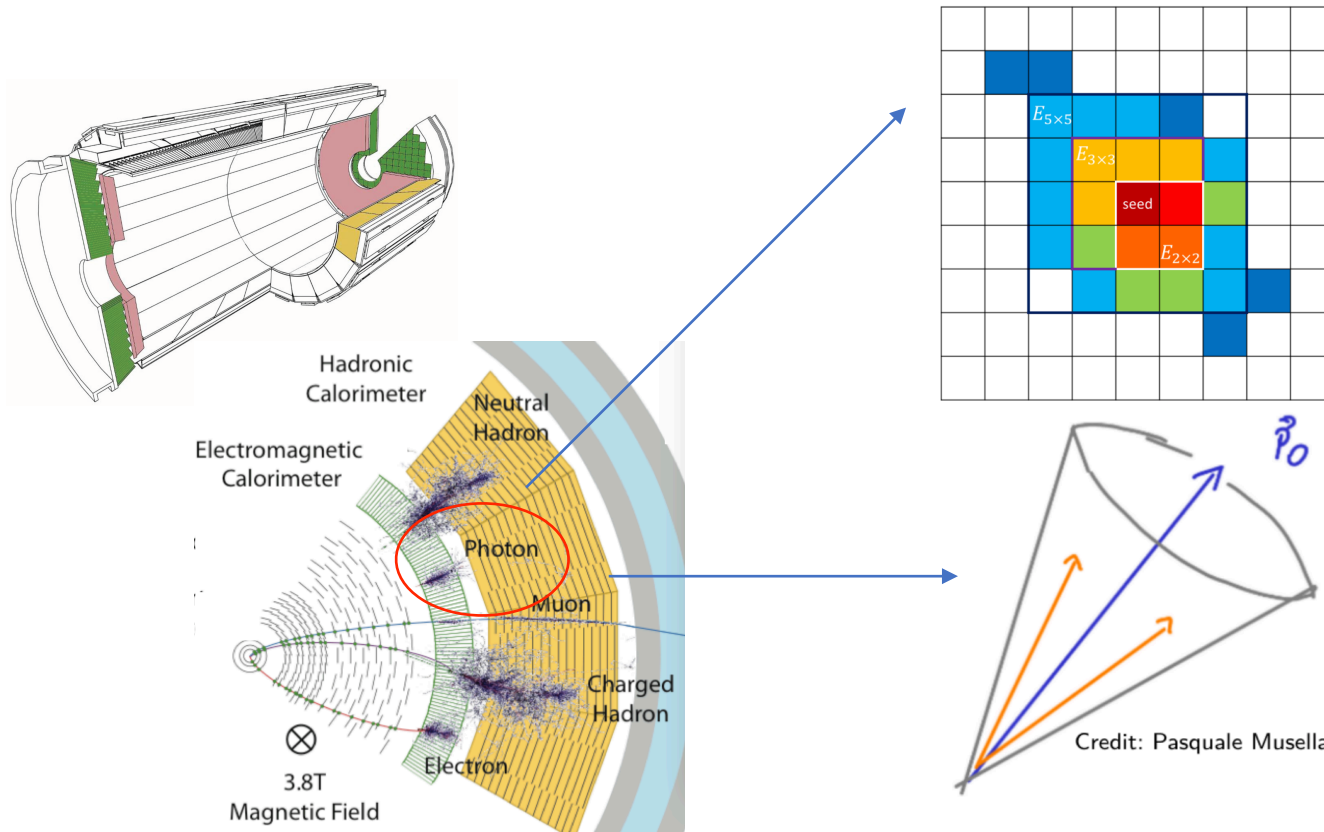
X. Chang, G. Dissertori, M. Donegá, M. Galli, P. Musella, S.
Pigazzini, T. Reitenspiess

22 March 2023



Simulation of Electromagnetic Variables

- Monte Carlo (MC) used in all the analyses with CMS data
- When it comes to analyses that use **photons** (e.g. $H \rightarrow \gamma\gamma$), the description of the **electromagnetic shower** in the ECAL is crucial:

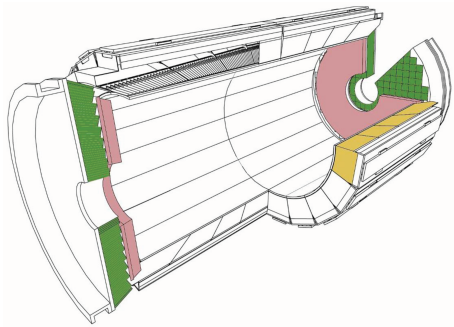


Shower shape variables: describe the shape of the EM shower cluster in the calorimeter

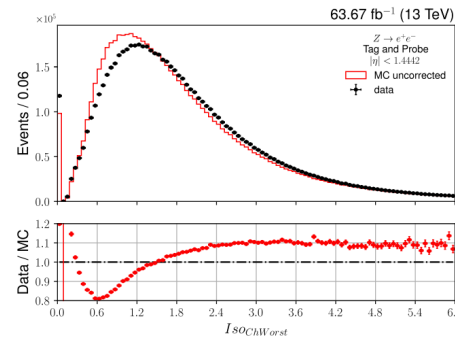
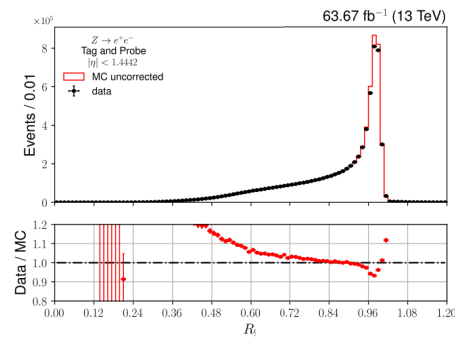
Isolation variables: characterize the activity around the object of interest

Simulation of Electromagnetic Variables

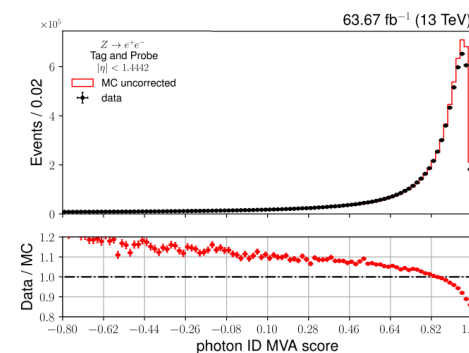
- Monte Carlo (MC) used in all the analyses with CMS data
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Detector aging makes it difficult to correctly simulate the shower development



Data - MC mismatch in shower shapes and isolation variables

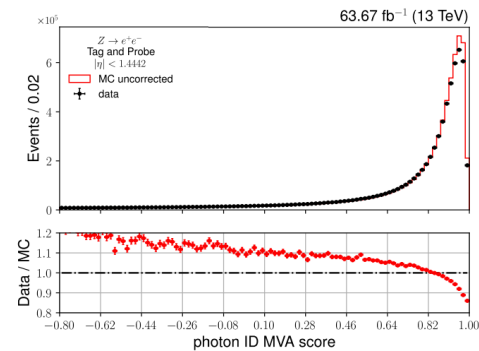
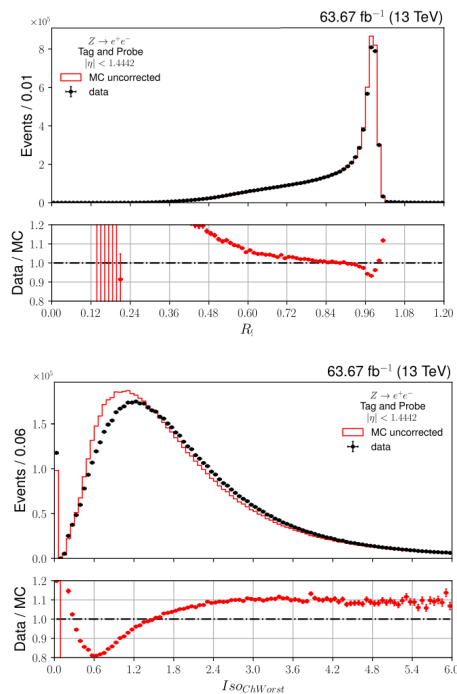


Disagreement propagated to **photon identification...**

... which ultimately results in **higher systematic uncertainties**

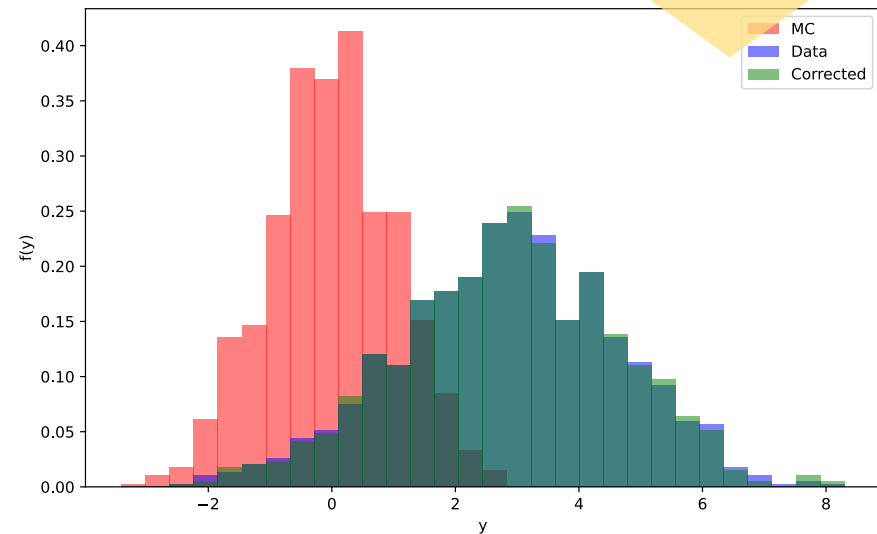
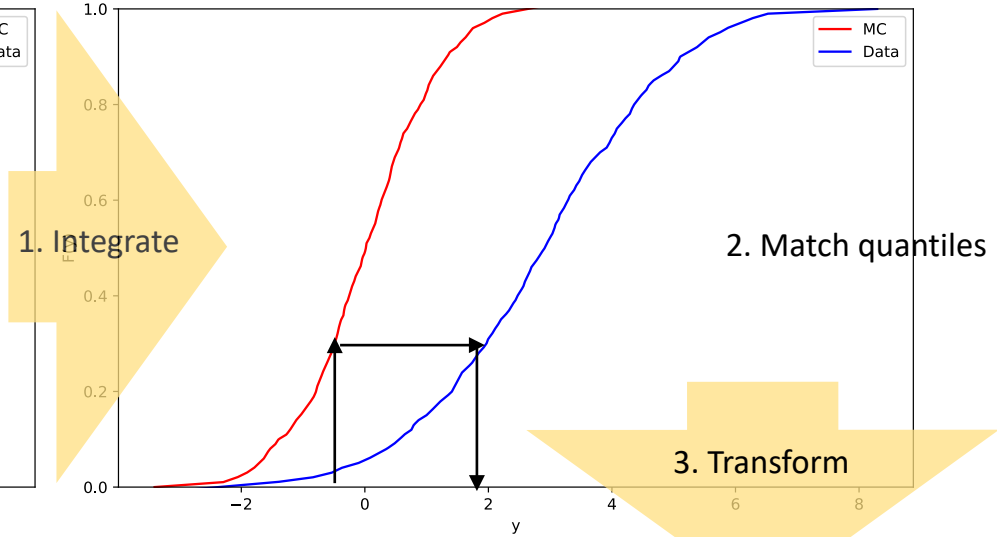
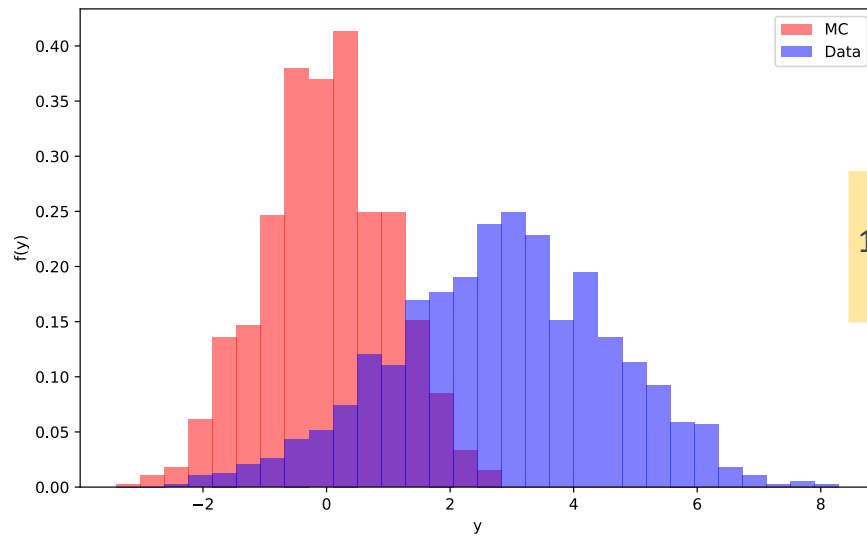
Simulation of Electromagnetic Variables

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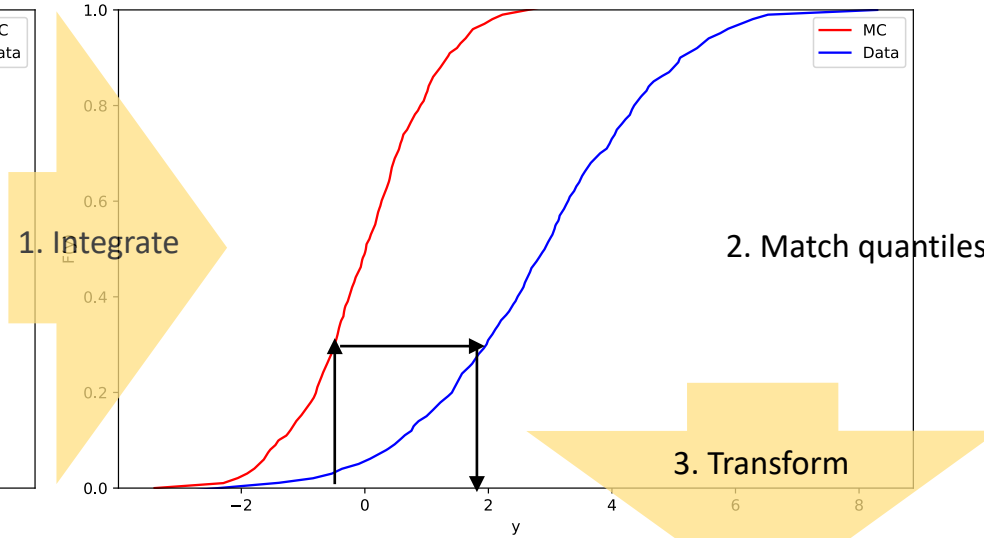
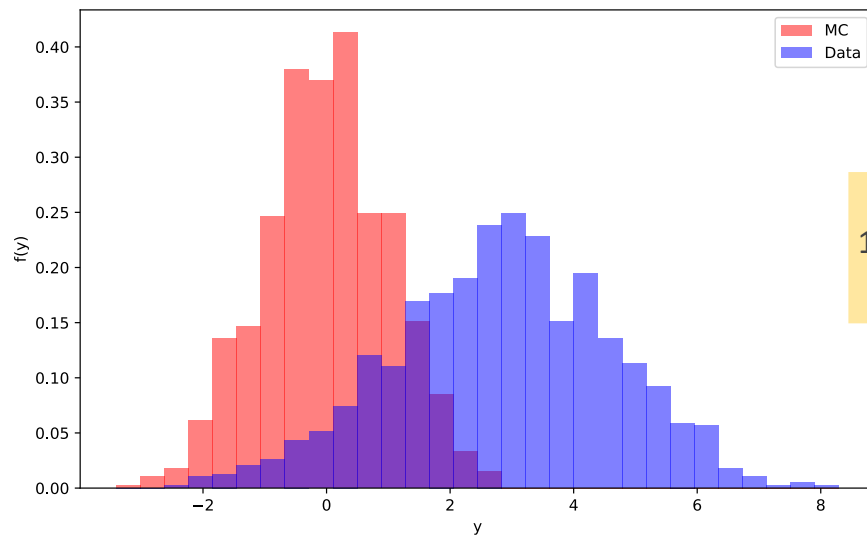


Developed a procedure called Chained Quantile Regression (**CQR**) to match MC with data (and hence decrease systematic uncertainties)

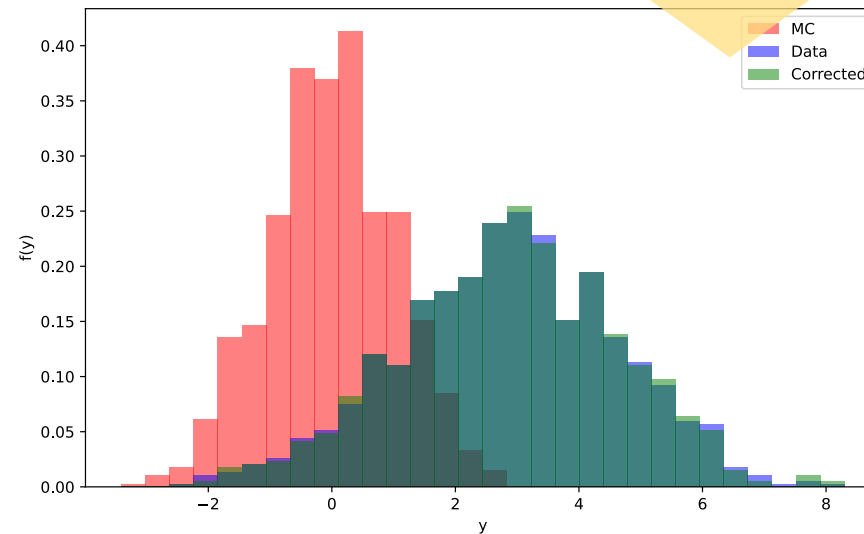
Quantile Morphing



Quantile Morphing

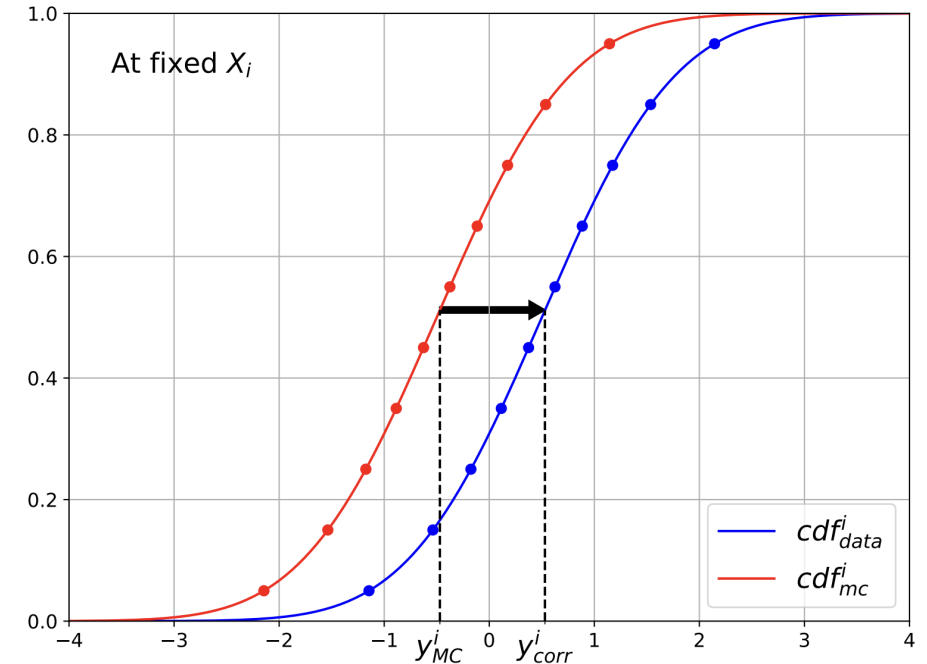


But we don't know the CDFs...



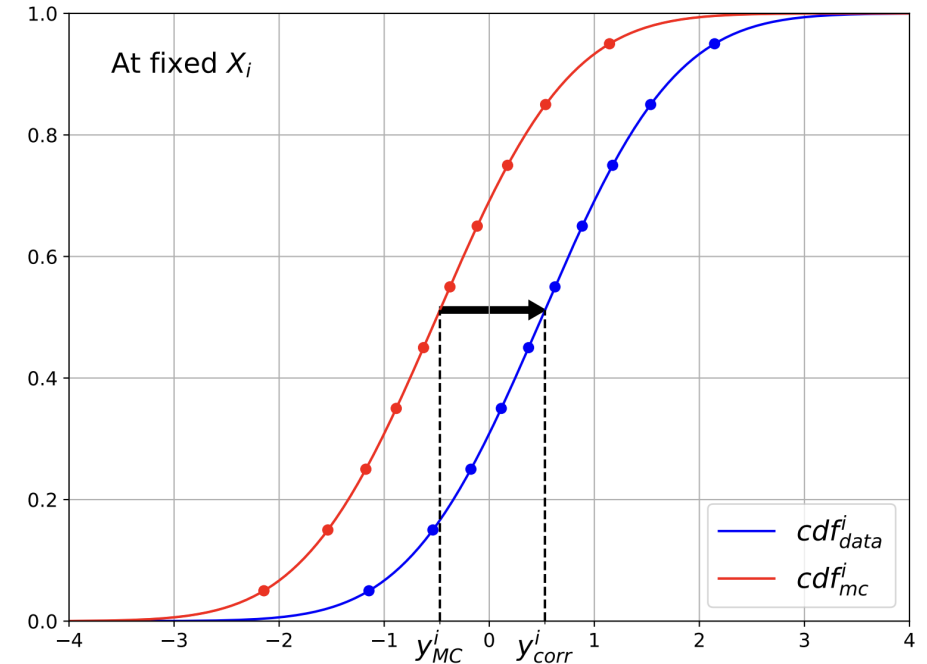
Quantile Regression

- Cumulative Distribution Function (**CDF**) of both data and MC depend on kinematic quantities $X = [p_t, \eta, \phi, \rho]$ - which describe the physics of the shower
- **Train regressors** to predict the conditional shape of CDFs using **21 quantiles**
- To correct a certain variable y_i^{MC} :
 - Find two quantiles around y_i^{MC} for data and MC
 - Use linear interpolation between the two points to obtain $cdf^{data}(y_i | X_i)$ and $cdf^{MC}(y_i | X_i)$
 - Compute $y_i^{MC,corr}$ by solving
$$y_i^{MC,corr} = cdf_{data}^{-1}(cdf^{MC}(y_i^{MC} | X_i))$$



Quantile Regression

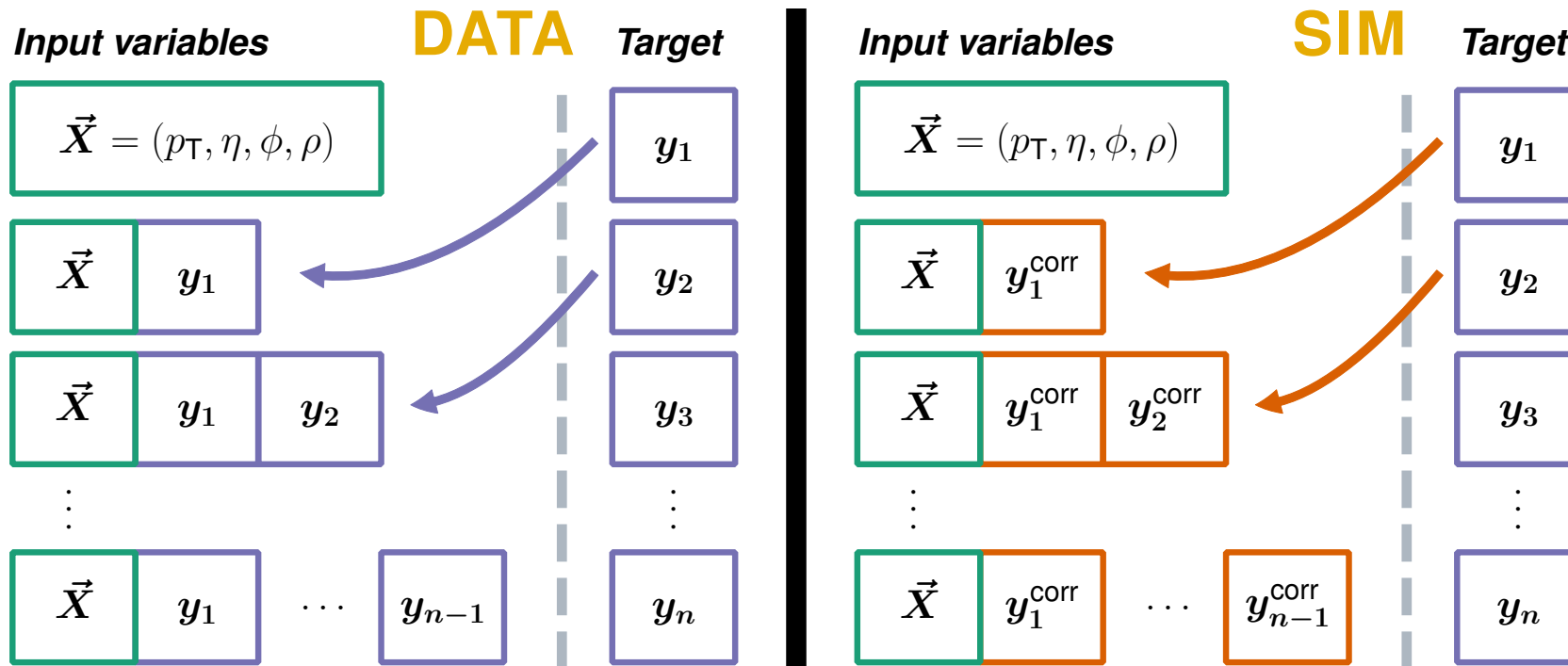
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But this is not enough because the variables are correlated...

Chained Quantile Regression

- In order to **catch correlations** between the variables we are correcting we need to chain them:
 - Data: for target variable y_i input variables are $X = [p_t, \eta, \phi, \rho, y_1, \dots, y_{i-1}]$
 - MC: for target variable y_i input variables are $X = [p_t, \eta, \phi, \rho, y_1^{corr}, \dots, y_{i-1}^{corr}]$



Chained Quantile Regression

y_1

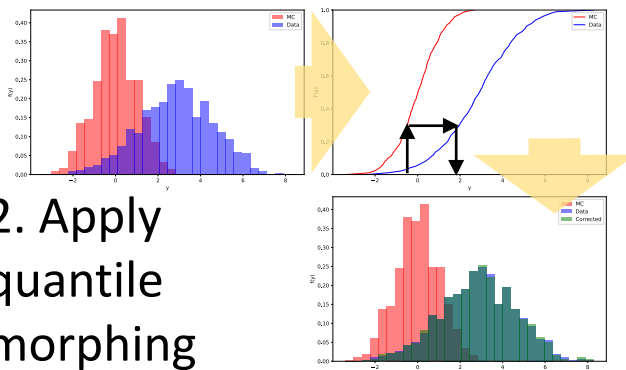
1. Train regressors to learn conditional CDF of **MC** and **data** for variable 1 using $X = [p_t, \eta, \phi, \rho]$ as input

y_i

Chained Quantile Regression

y_1

2. Apply
quantile
morphing



1. Train regressors to learn conditional CDF of **MC** and **data** for variable 1 using $X = [p_t, \eta, \phi, \rho]$ as input

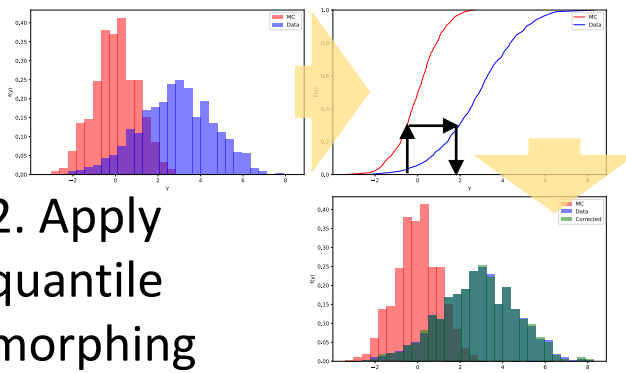
y_i

Chained Quantile Regression

y_1

1. Train regressors to learn conditional CDF of **MC** and **data** for variable 1 using $X = [p_t, \eta, \phi, \rho]$ as input

2. Apply quantile morphing



3. Repeat the procedure for variable i using

$X = [p_t, \eta, \phi, \rho, y_1, \dots, y_{i-1}]$
(data)

$X = [p_t, \eta, \phi, \rho, y_1^{corr}, \dots, y_{i-1}^{corr}]$
(MC) as input

y_i

What are these regressors?

In its first implementation (still used in most $H \rightarrow \gamma\gamma$ analyses) **one BDT per quantile** was trained:

21 BDTs
x 9 variables
x 2 samples
x 2 detector parts
+ (...)
= many BDTs!

Computationally
expensive and time
consuming!

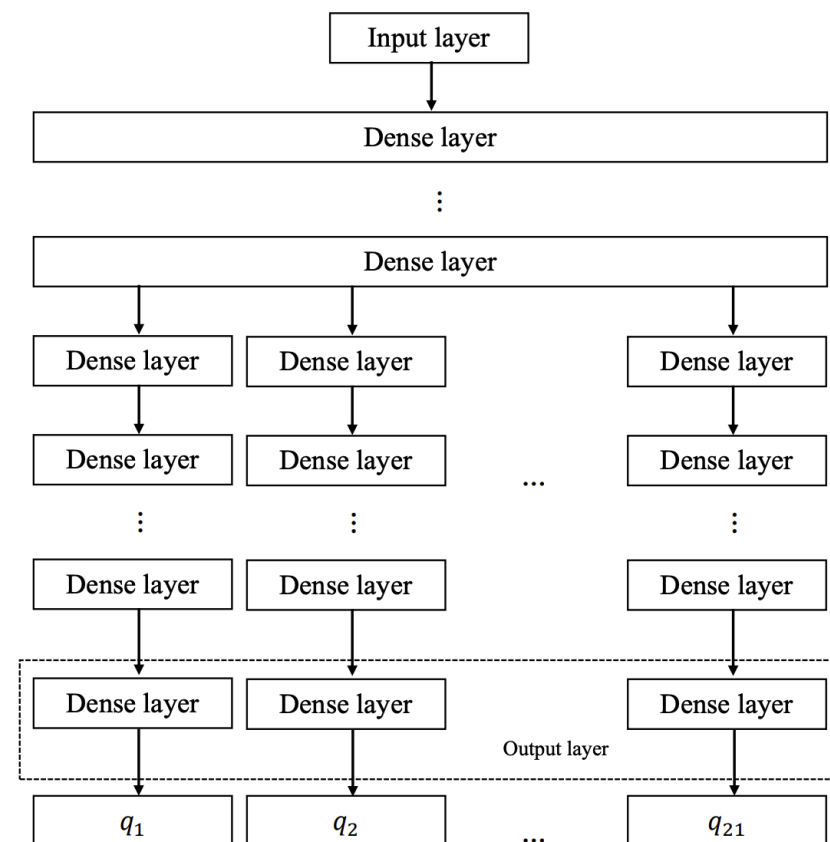
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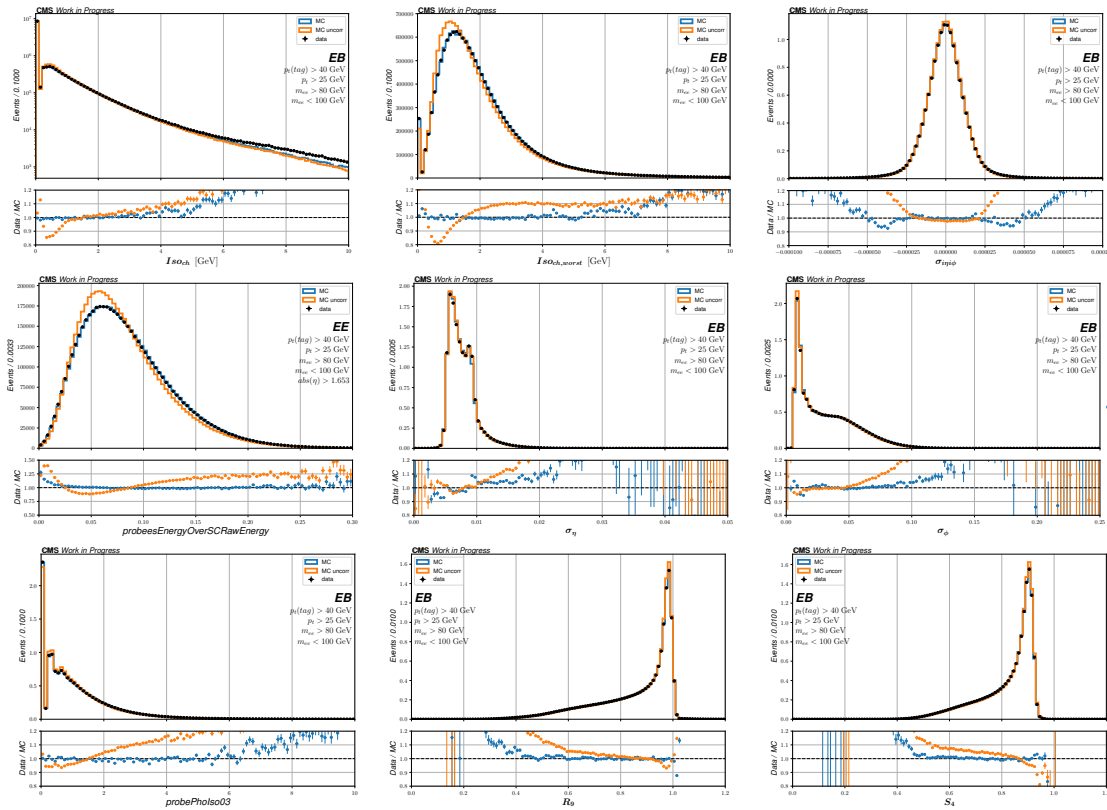
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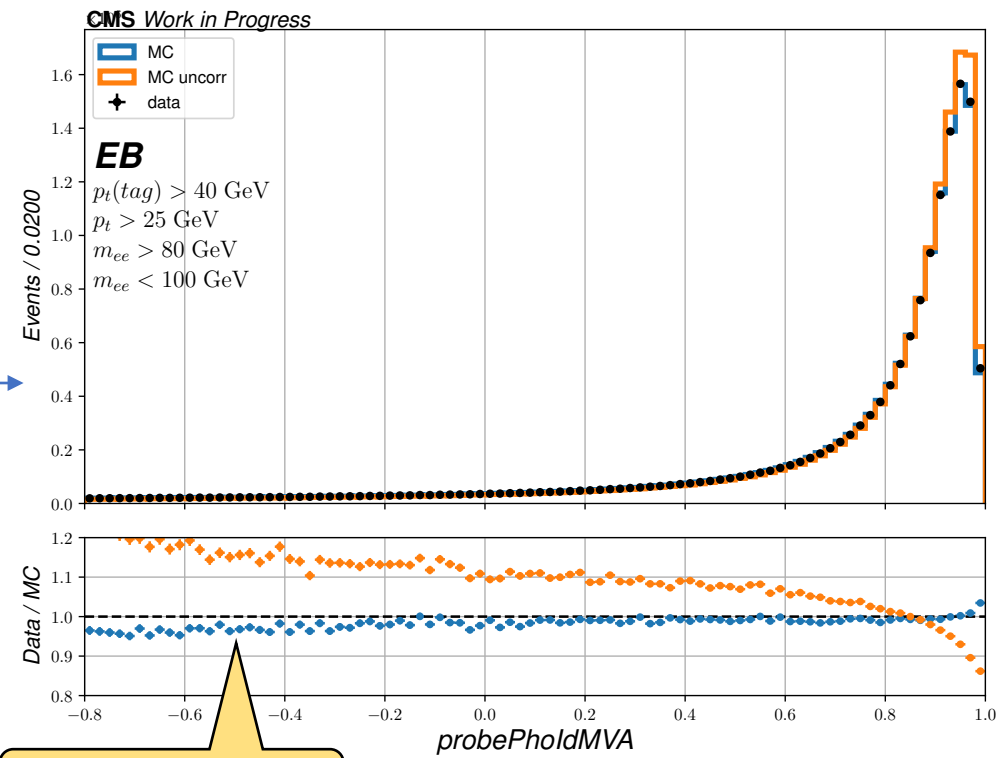
In a second iteration of the work the 21 BDTs of each variable were replaced by a single **quantile regression neural network**:



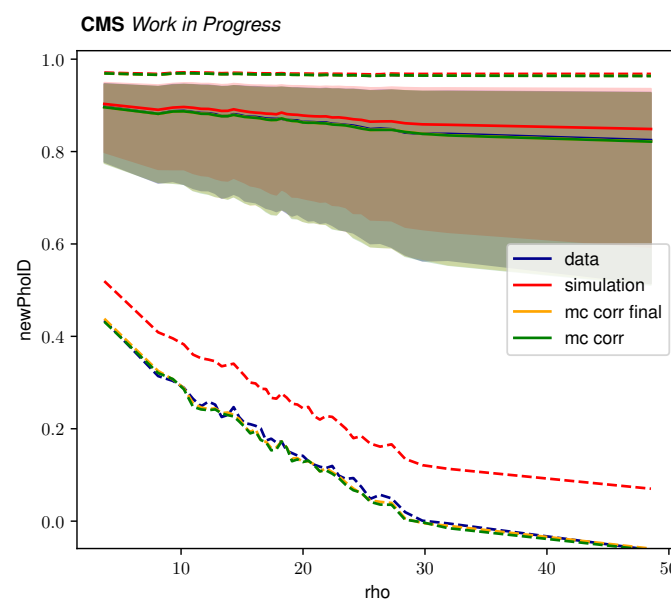
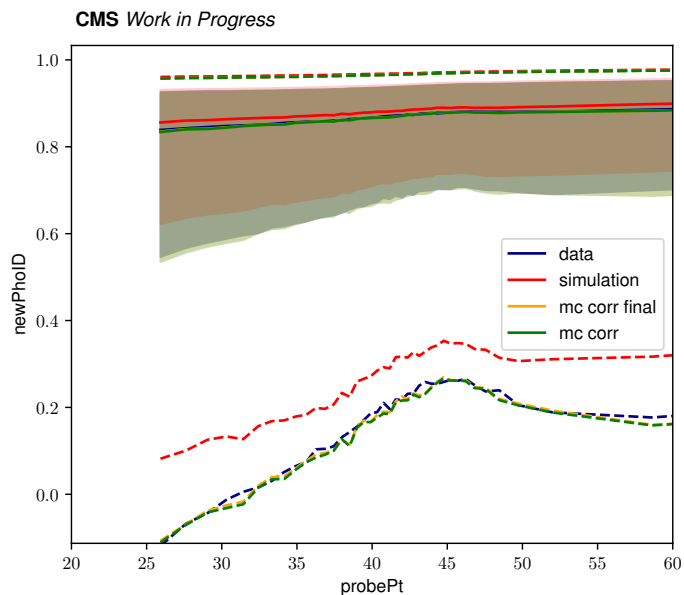
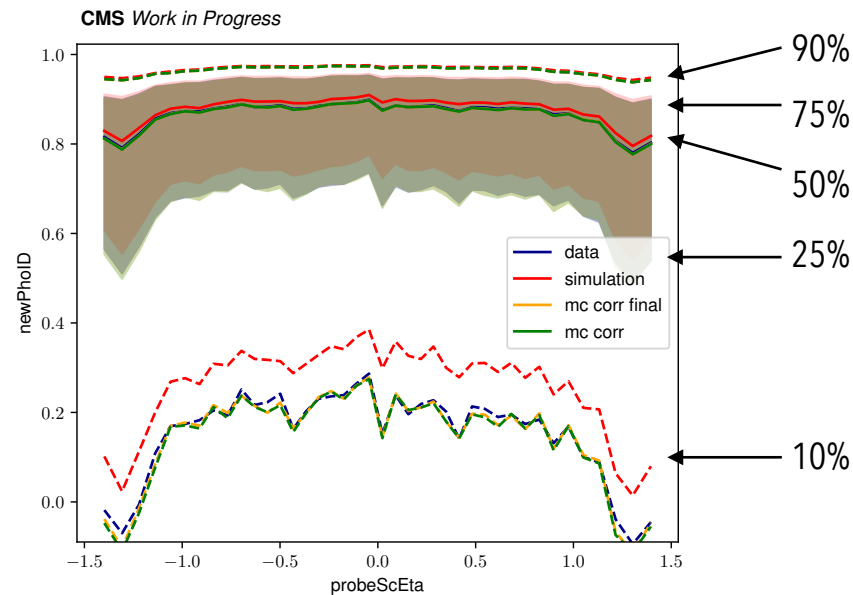
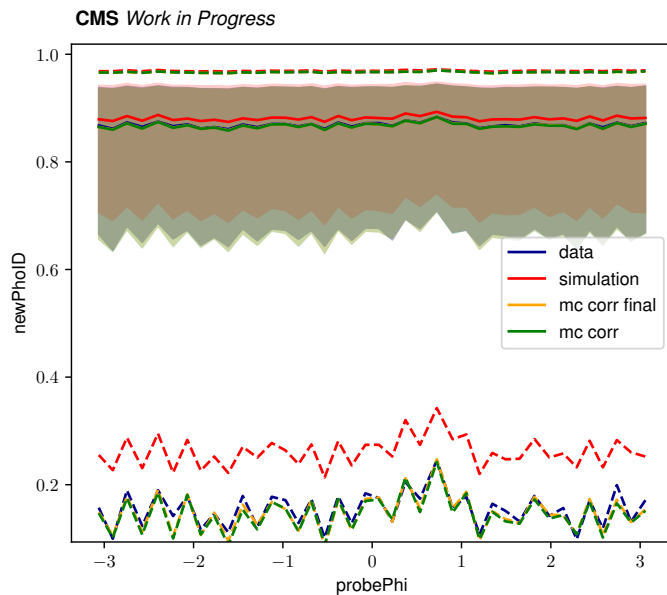
Corrected Distributions



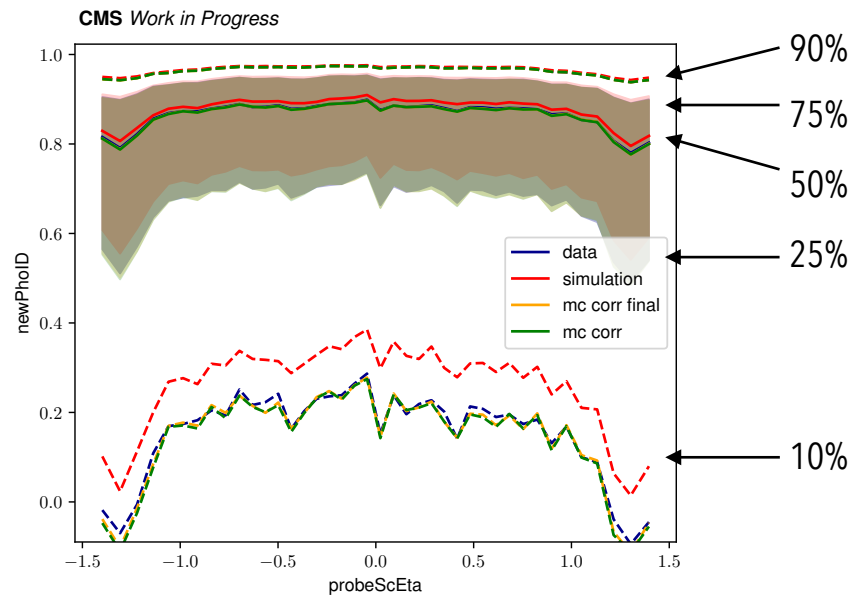
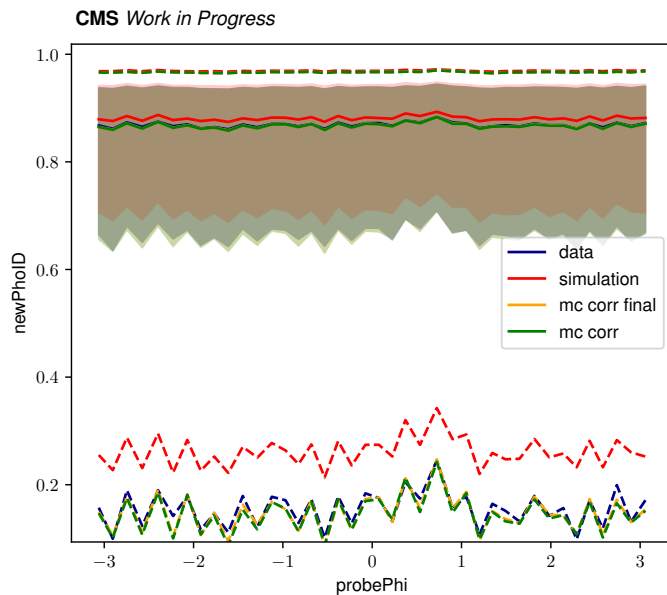
ID MVA



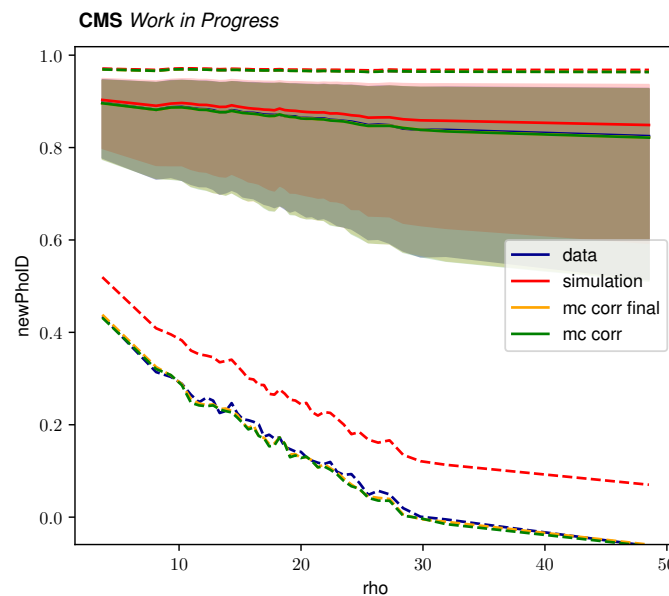
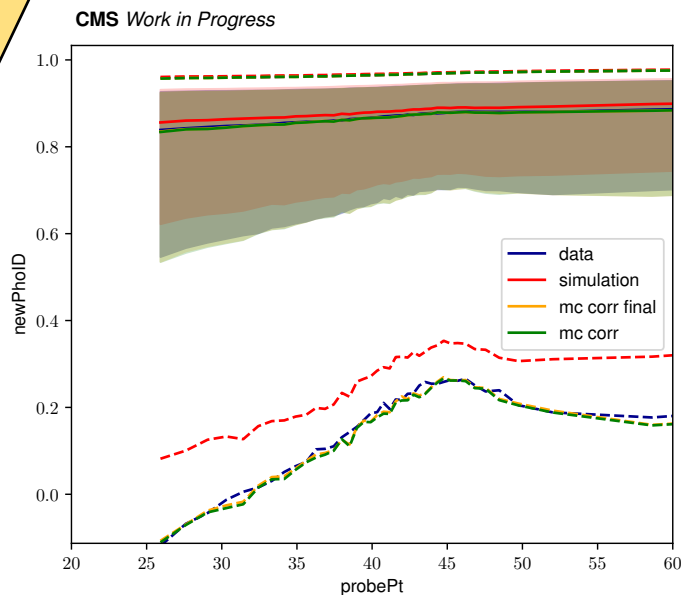
Profiles



Profiles

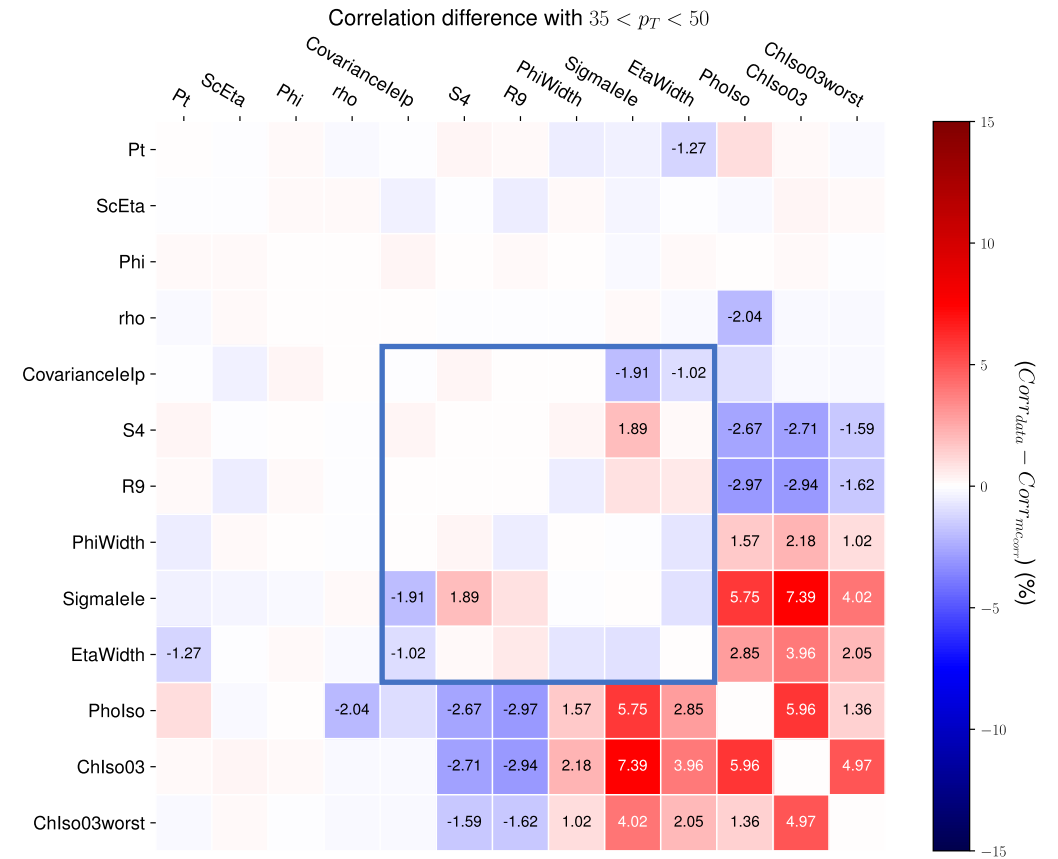
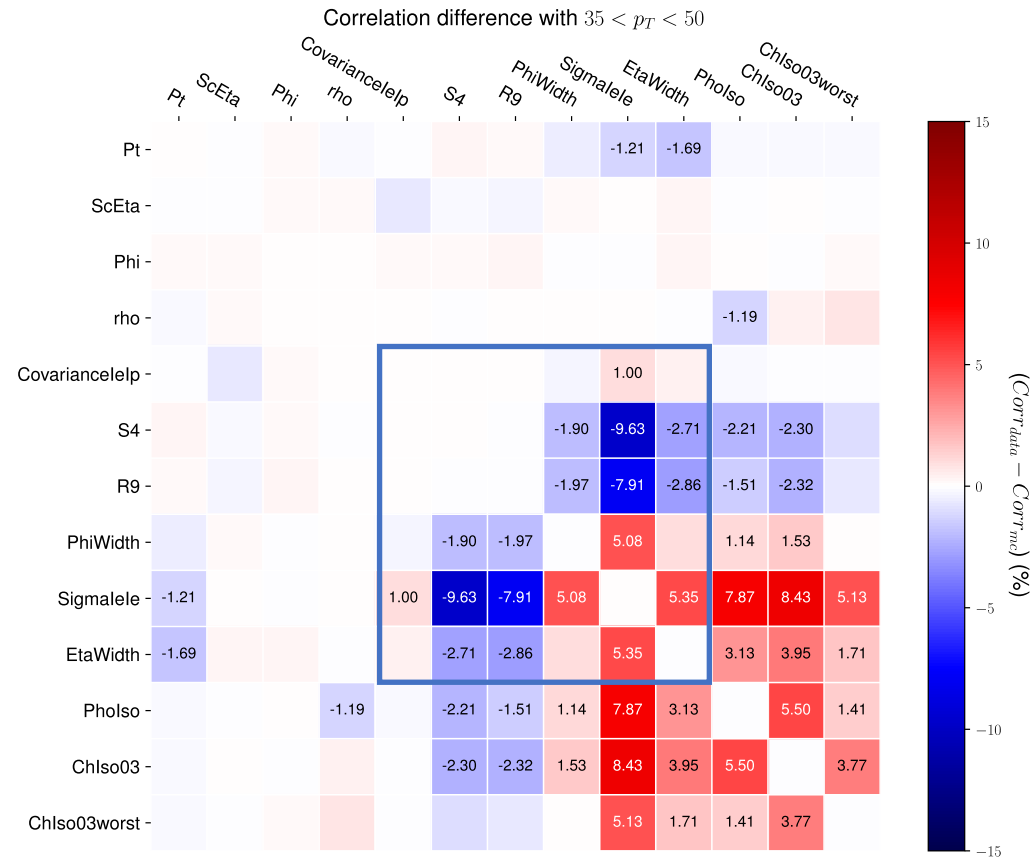


Closer agreement between data and MC corrected profiles



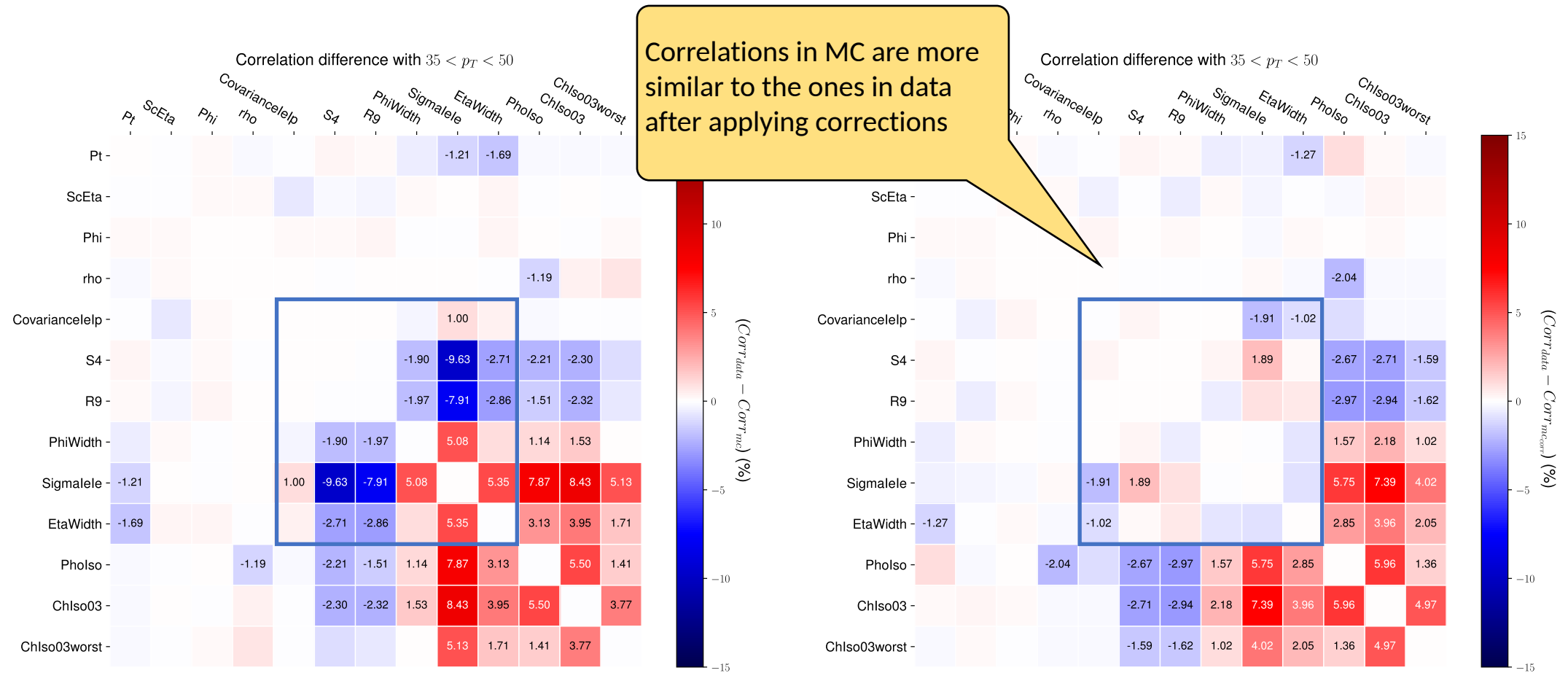
Correlations

Difference of correlation matrices between data and MC **before** (left) and **after** (right) corrections:



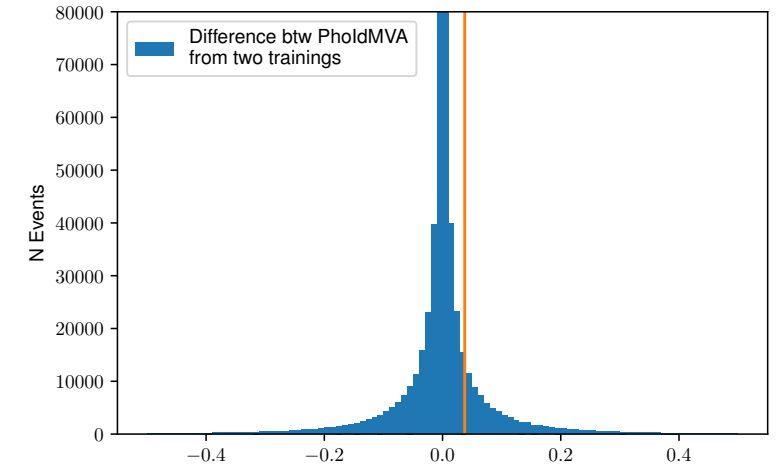
Correlations

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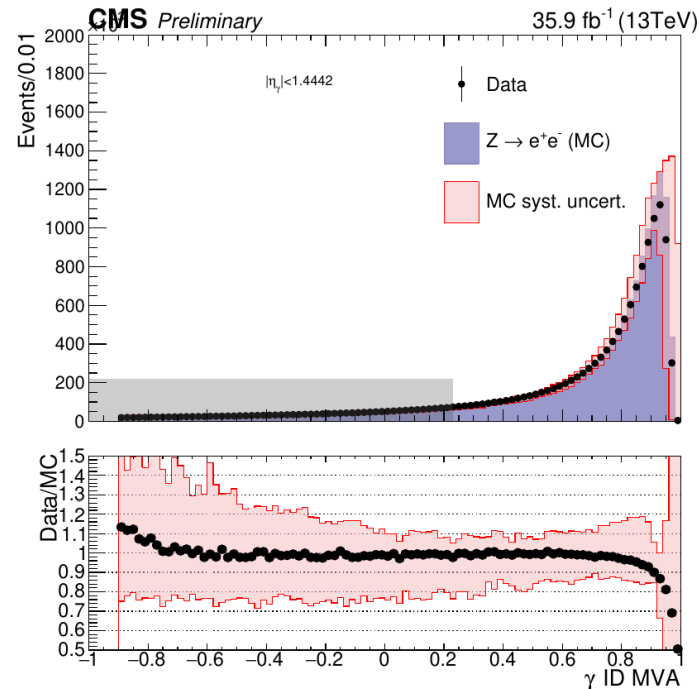


Systematic Uncertainties

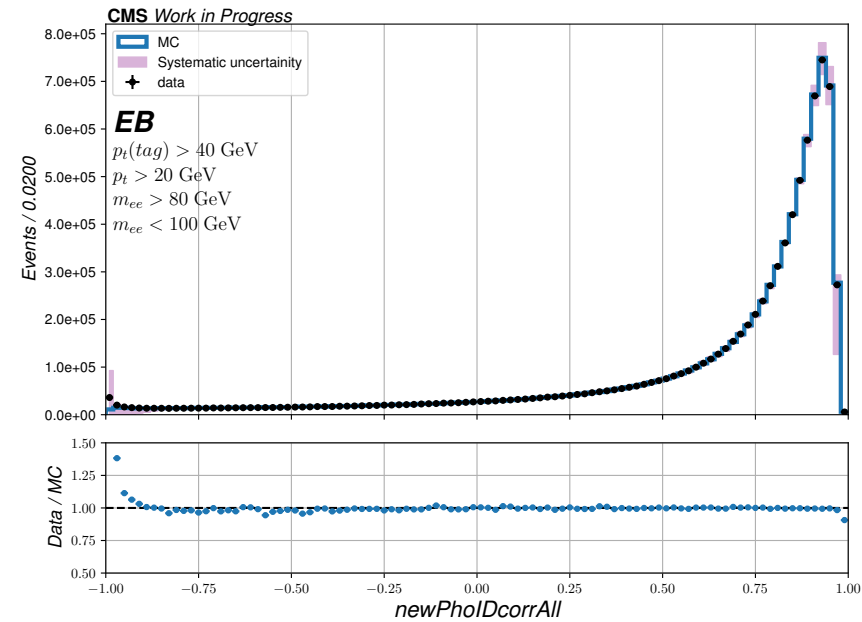
- Correction scheme accounts for all uncertainties and correlations → the only uncertainty comes from **finite size** of training sample
- Split the training sample in two and derive $\pm 1\sigma$ from the RMS of the $PhoID_1 - PhoID_2$ distribution



Run 1 Analysis (no corrections)



Run 2 Analysis



Future Prospects: Normalizing Flows

Also in its NN implementation, the CQR requires to train models and regressors one after the other to **take correlations into consideration**

Takes a long time and the corrected distributions need to be checked at every step

Normalizing flows allow to model high dimensional conditional distributions (see [D. Valsecchi's talk](#))

Benefit: chain is removed, making the training simpler and faster

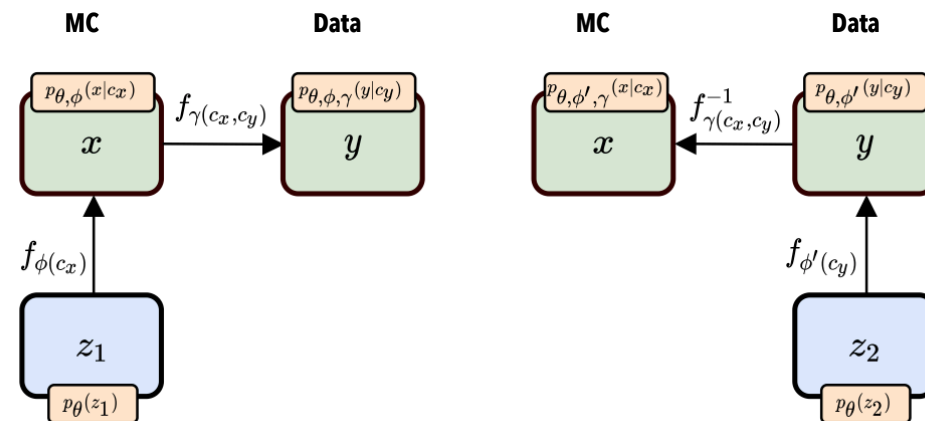
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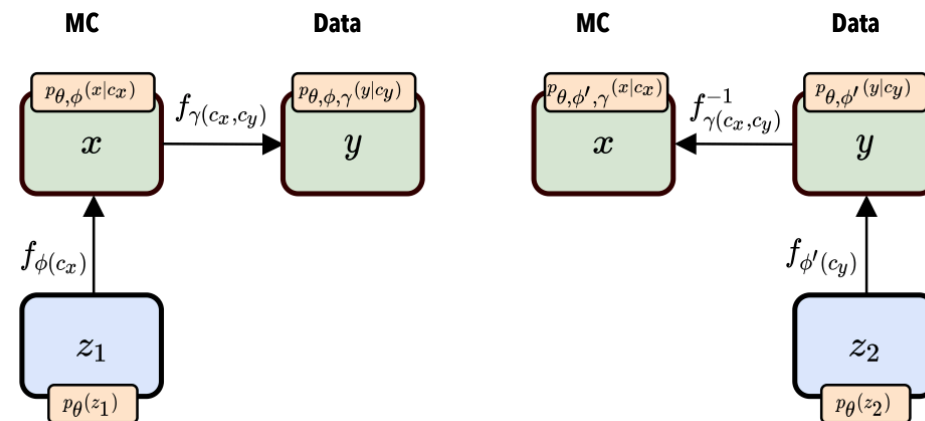
From Flow4Flow [paper](#)

As showed in [arXiv:2211.02487](#) it is possible to train a system of three normalizing flows able to map two multidimensional conditional distributions into one another...

But does this procedure reach the level of precision that we require?

Future Prospects: Normalizing Flows

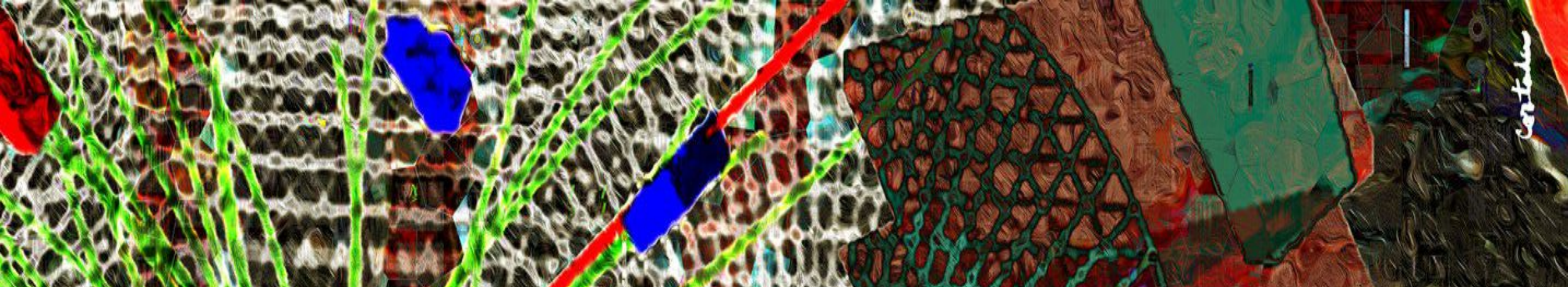
If you find this idea interesting and you want to work on it, we are offering this as a semester project - **Contact us!**



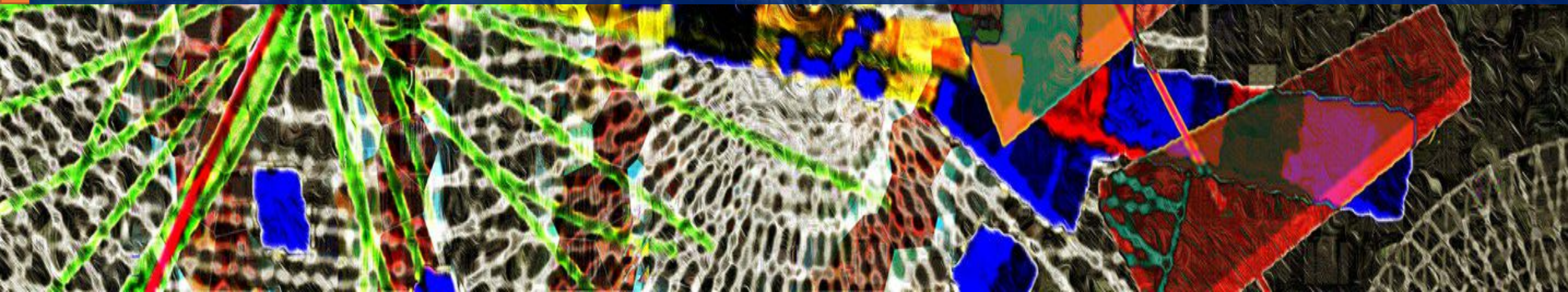
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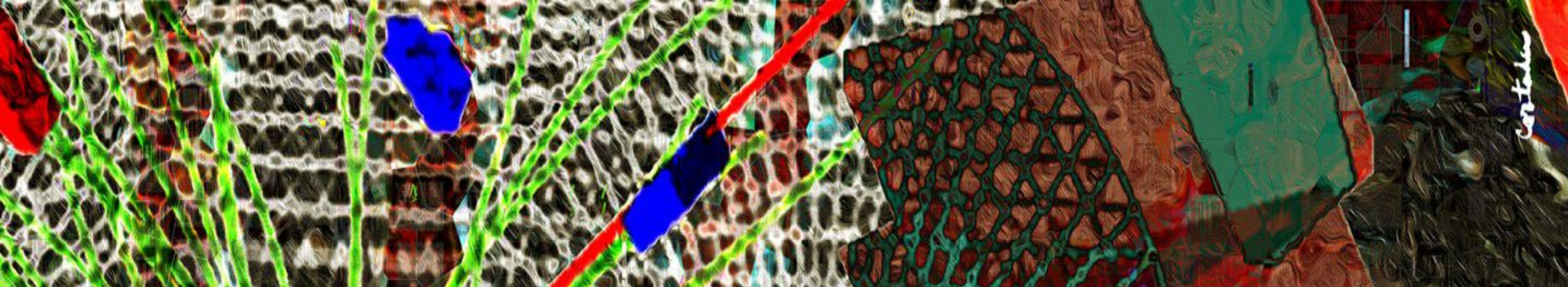
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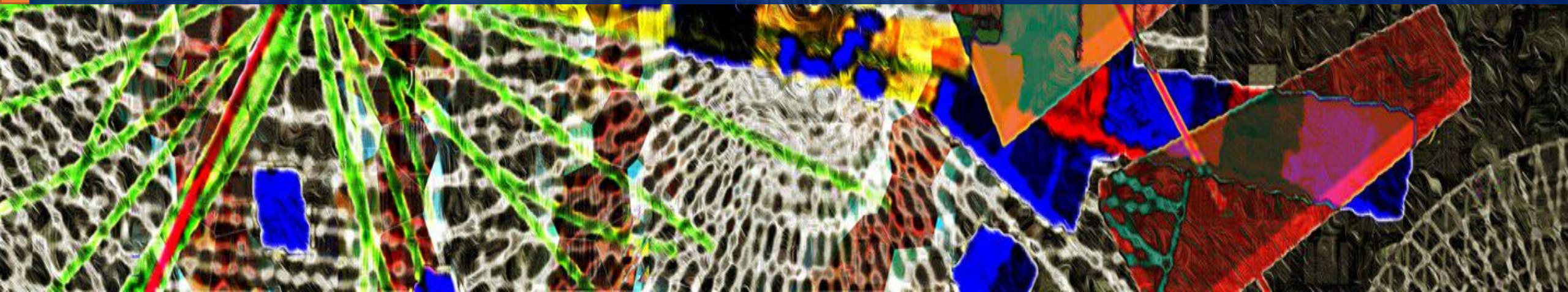


Thank you for your attention!





Backup



Correction Approach

- Developed procedure called **Chained Quantile Regression (CQR)** to match data with MC (and hence decrease systematic uncertainties)
- Corrections are derived using Tag & Probe method on $Z \rightarrow e^+e^-$ events, with the reconstruction of the probe leg as a photon
- PhotonID score is re-evaluated with corrected variables

